

# MatCalc

Engineering

## “ABC”-models for subgrain structure evolution in MatCalc 6

(MatCalc 6.00.0258)

P. Warczok



# Outlook

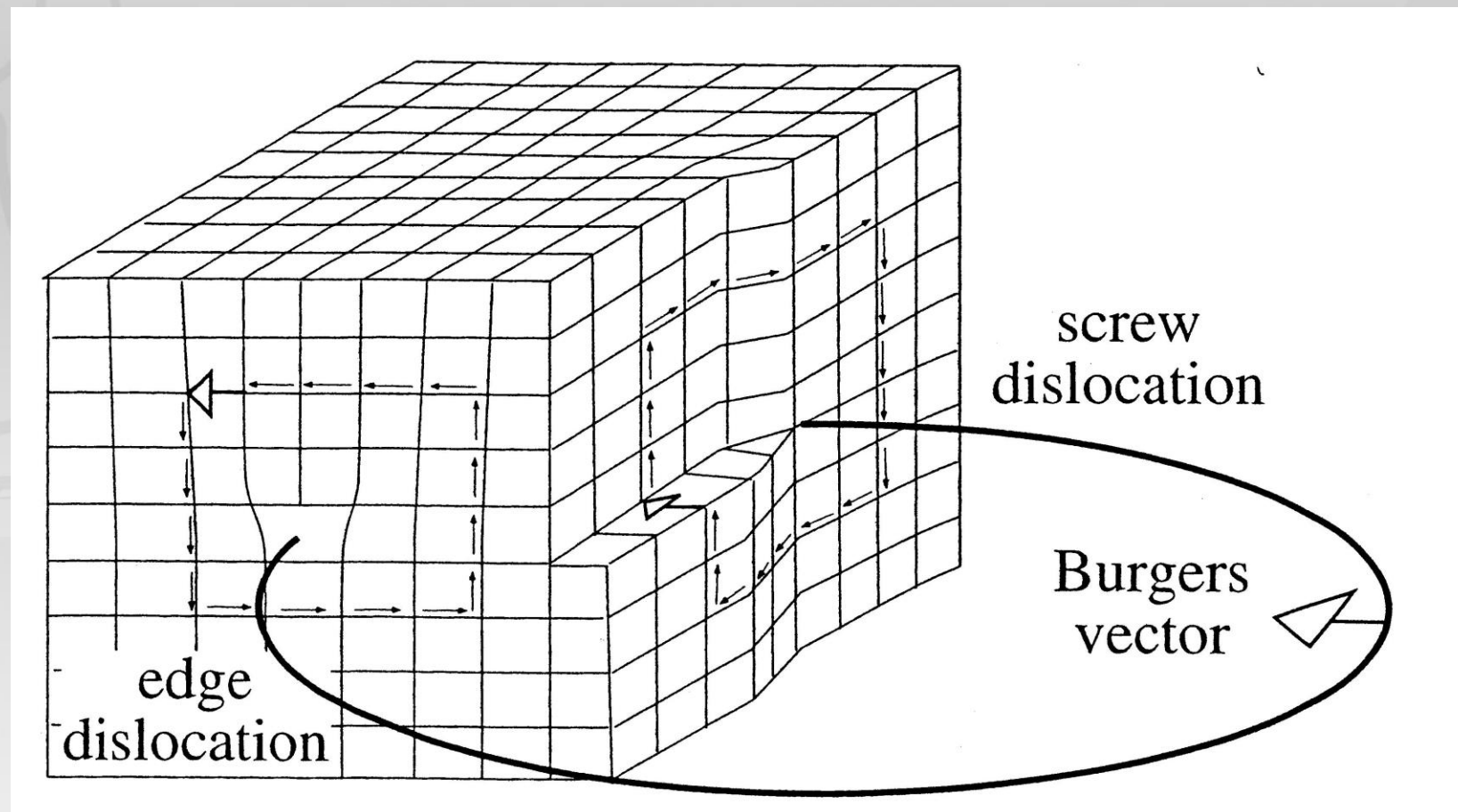
- Few words on substructure
- Dislocation density evolution model
- Subgrain size evolution model
- Model demonstration



# Introduction to dislocations

# Dislocations

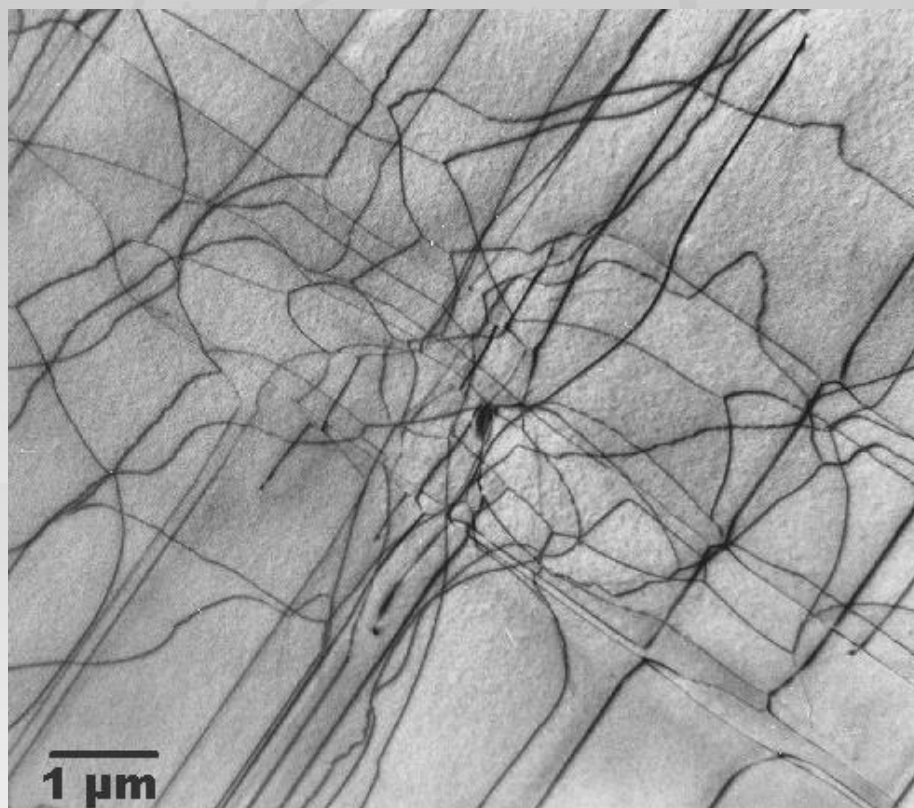
- Two geometries:
  - Edge
  - Screw



<http://www.geology.um.maine.edu/geodynamics/AnalogWebsite/UndergradProjects2010/PatrickRyan/Content/dislocationdiagram.jpg>

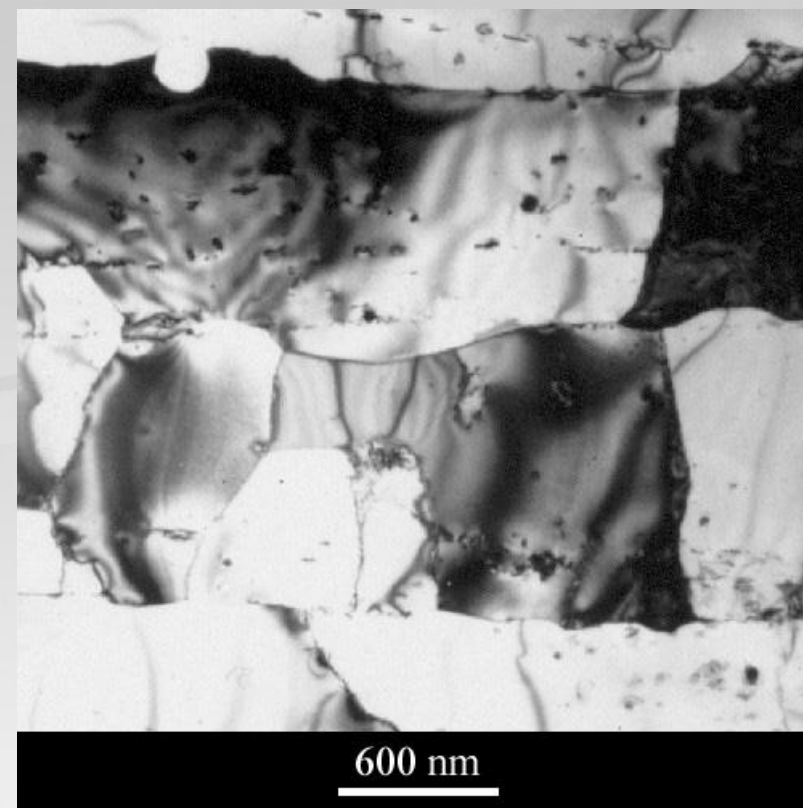
# Dislocations

## Internal dislocations



[https://www.tf.uni-kiel.de/matwis/amat/iss/kap\\_5/illustr/misfit\\_dislocations\\_si.gif](https://www.tf.uni-kiel.de/matwis/amat/iss/kap_5/illustr/misfit_dislocations_si.gif)

## Wall dislocations



<https://www.flickr.com/photos/core-materials/3840257277>

# Dislocations & subgrains

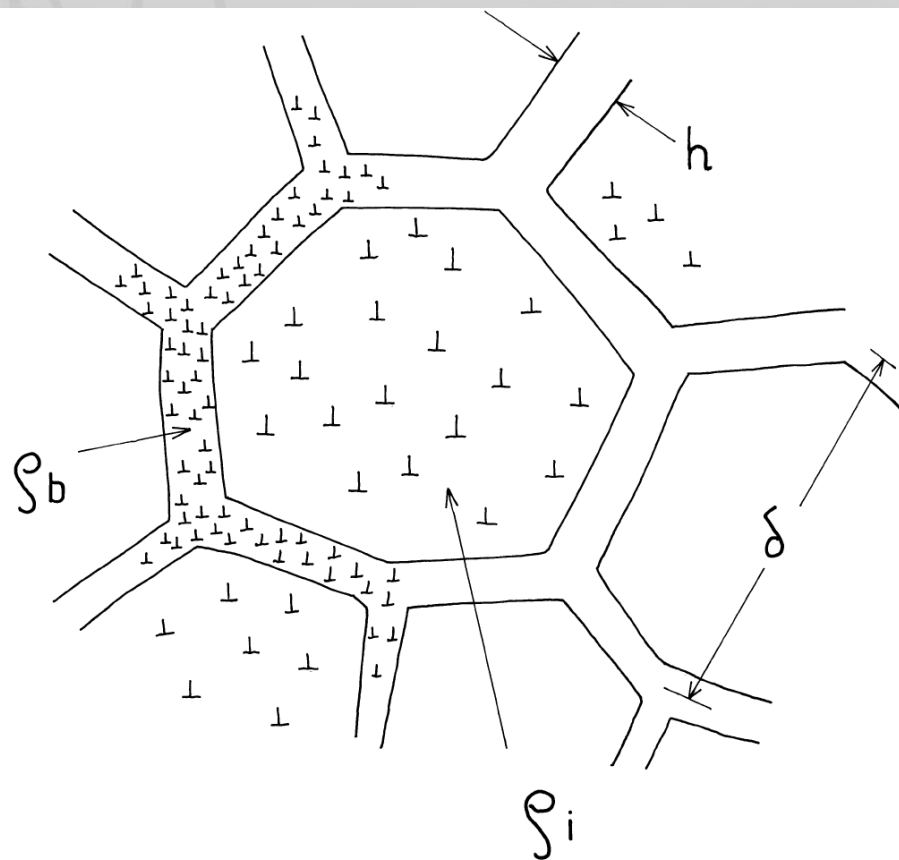


Fig. 7. A schematic representation of the microstructure; cell diameter,  $\delta$ , cell wall thickness,  $h$ , cell wall dislocation density,  $\rho_b$  and dislocation density within the cells,  $\rho_i$

E. Nes, Prog. Mater. Sci. 41 (1998) p.129-193

# Dislocation density

- Impact:
  - Diffusion (pipe-diffusion)
  - Nucleation rate (number of nucleation sites)
  - Subgrain size (through similitude principle)
  - Recrystallization onset
  - Yield strength
    - Directly - work hardening
    - Indirectly – subgrain size, precipitate size



# Dislocation density evolution



# Dislocation density evolution

- Stress in material increases with dislocation density
- Flow curve analysis
  - Various stages in dislocation density evolution
  - Dislocation density saturation expected at some point

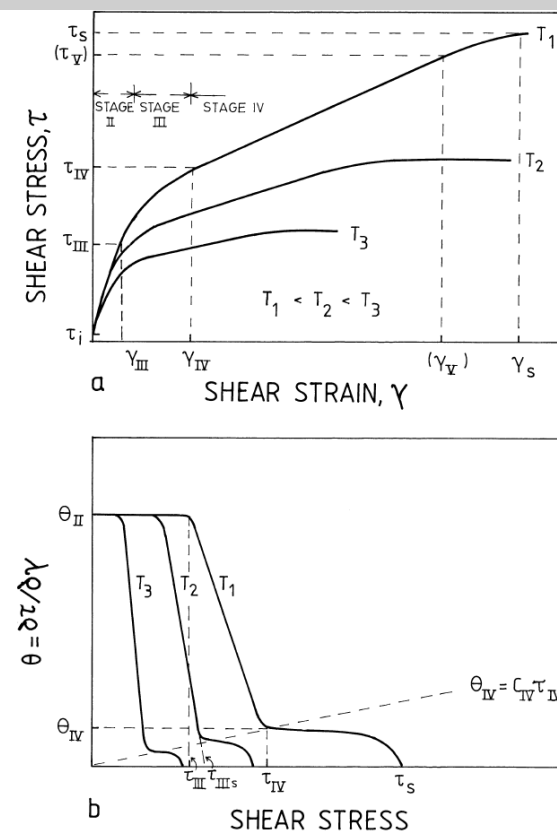
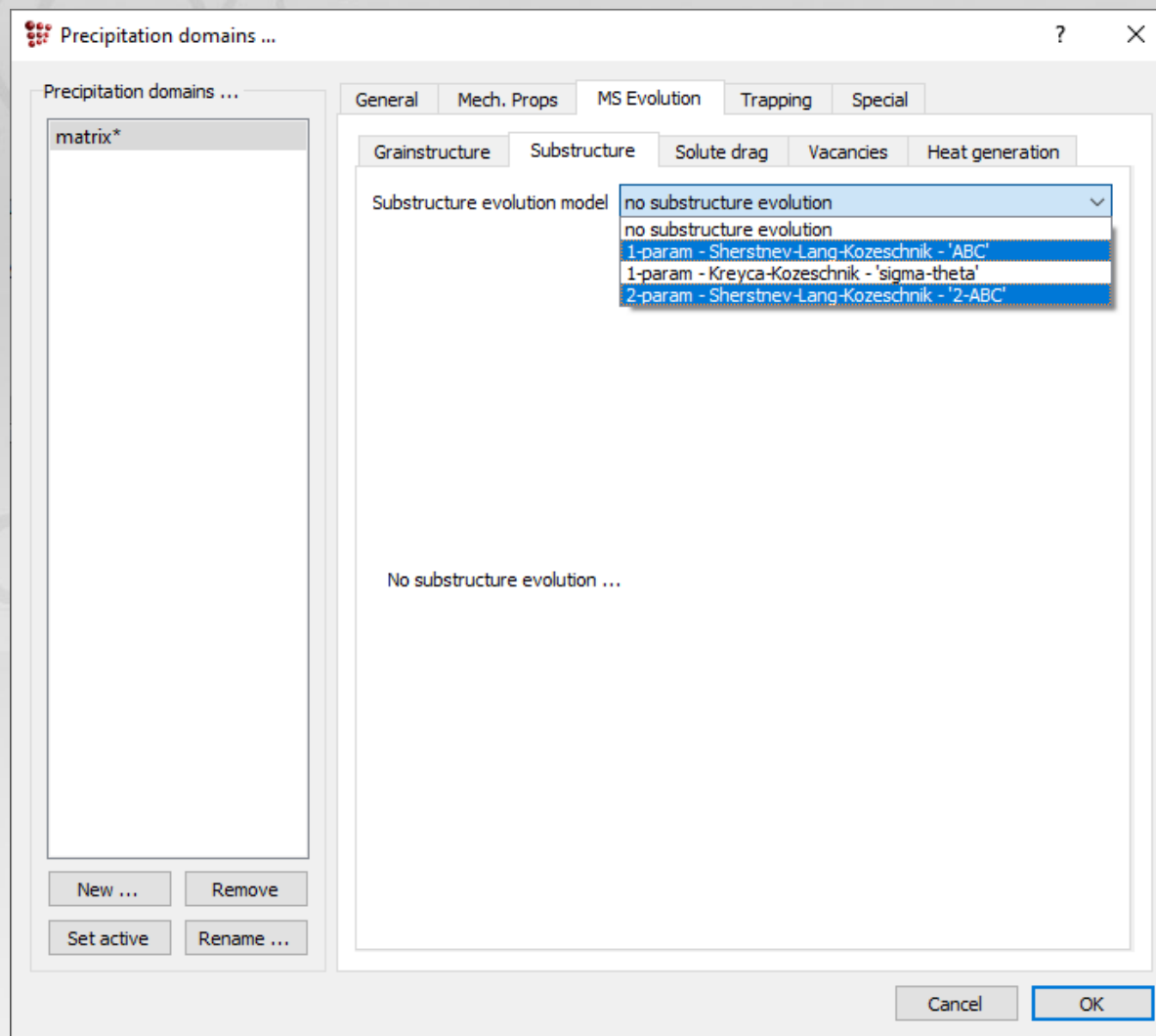


Fig. 1. (a) Schematic stress–strain curves and (b) strain hardening ( $\theta$ ) vs flow stress ( $\tau$ ) curves for fcc-metals

# Dislocation density evolution

- MatCalc models
  - Sherstnev-Lang-Kozeschnik (SLK) models
    - 1 parameter model (a.k.a. „1ABC“)
    - 2 parameters model (a.k.a. „2ABC“)
  - 1 parameter model: global dislocation density evolution
  - 2 parameters model: separate dynamics for intrinsic and wall dislocations

# Dislocation density evolution



# Dislocation density evolution

$$\dot{\rho} = \dot{\rho}_1 - \dot{\rho}_2 - \dot{\rho}_3$$

- Dislocation generation
  - Deformation  $\rightarrow \dot{\rho}_1$
- Dislocation annihilation
  - Dynamic recovery (dislocations with antiparallel Burgers vectors hit each other)  $\rightarrow \dot{\rho}_2$
  - Static recovery (dislocation climb)  $\rightarrow \dot{\rho}_3$

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# Dislocation generation (deformation)

$$\dot{\rho}_1 = A^{-1} \frac{M}{b} \dot{\varepsilon} \sqrt{\rho}$$

$\rho$  - Dislocation density

$A$  - A-parameter (constant)

$M$  - Taylor factor

$\dot{\varepsilon}$  - Strain rate

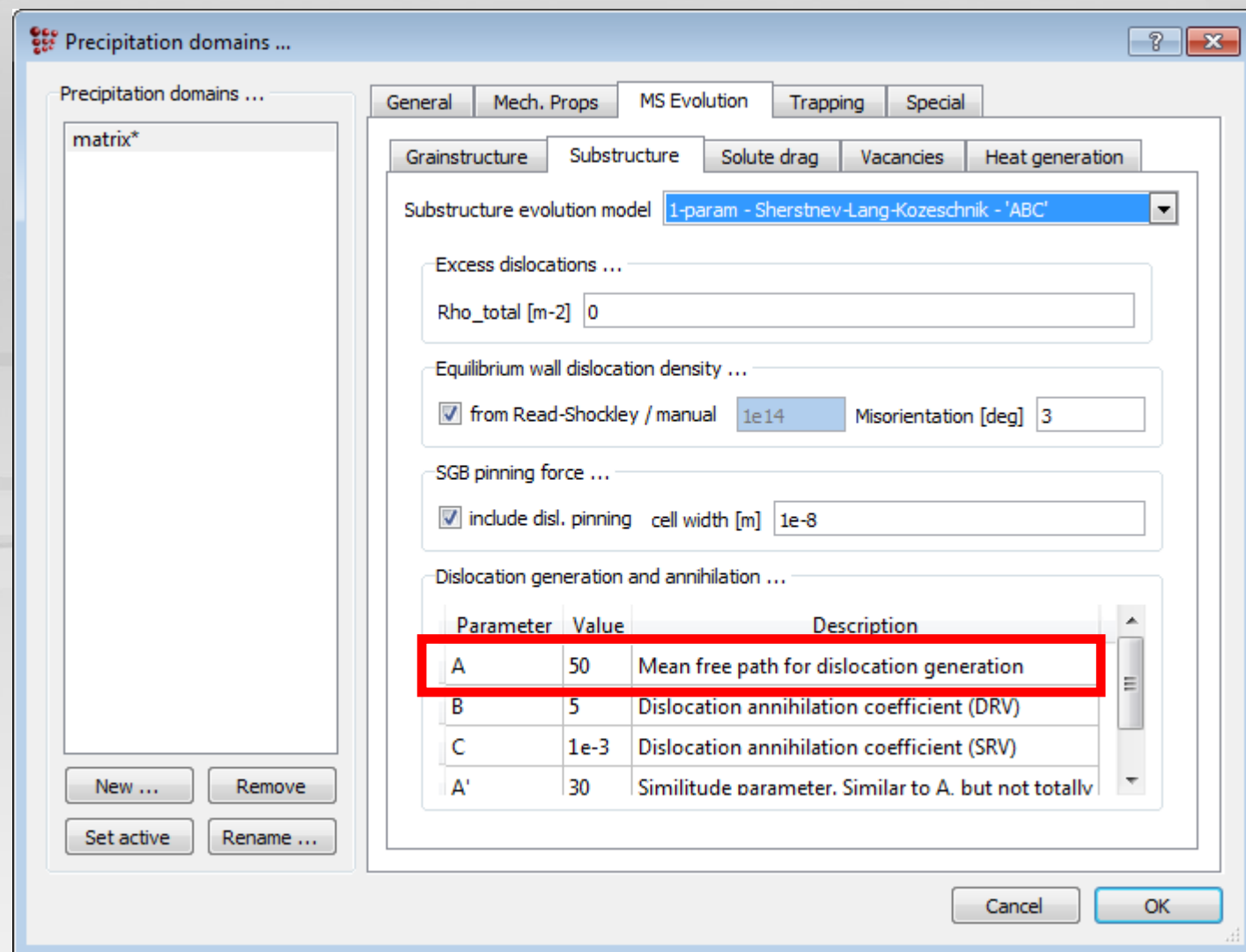
$b$  - Burgers vector

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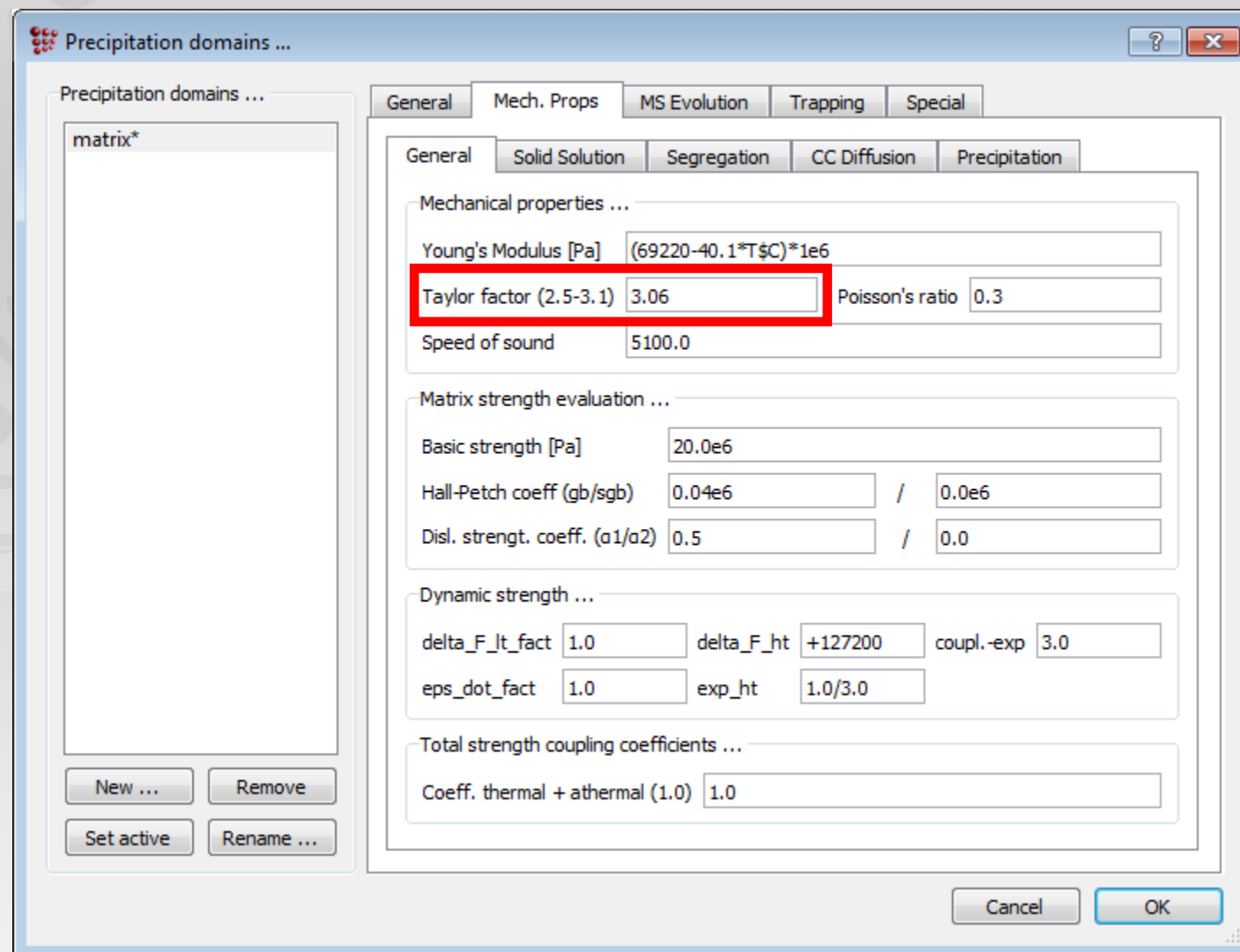
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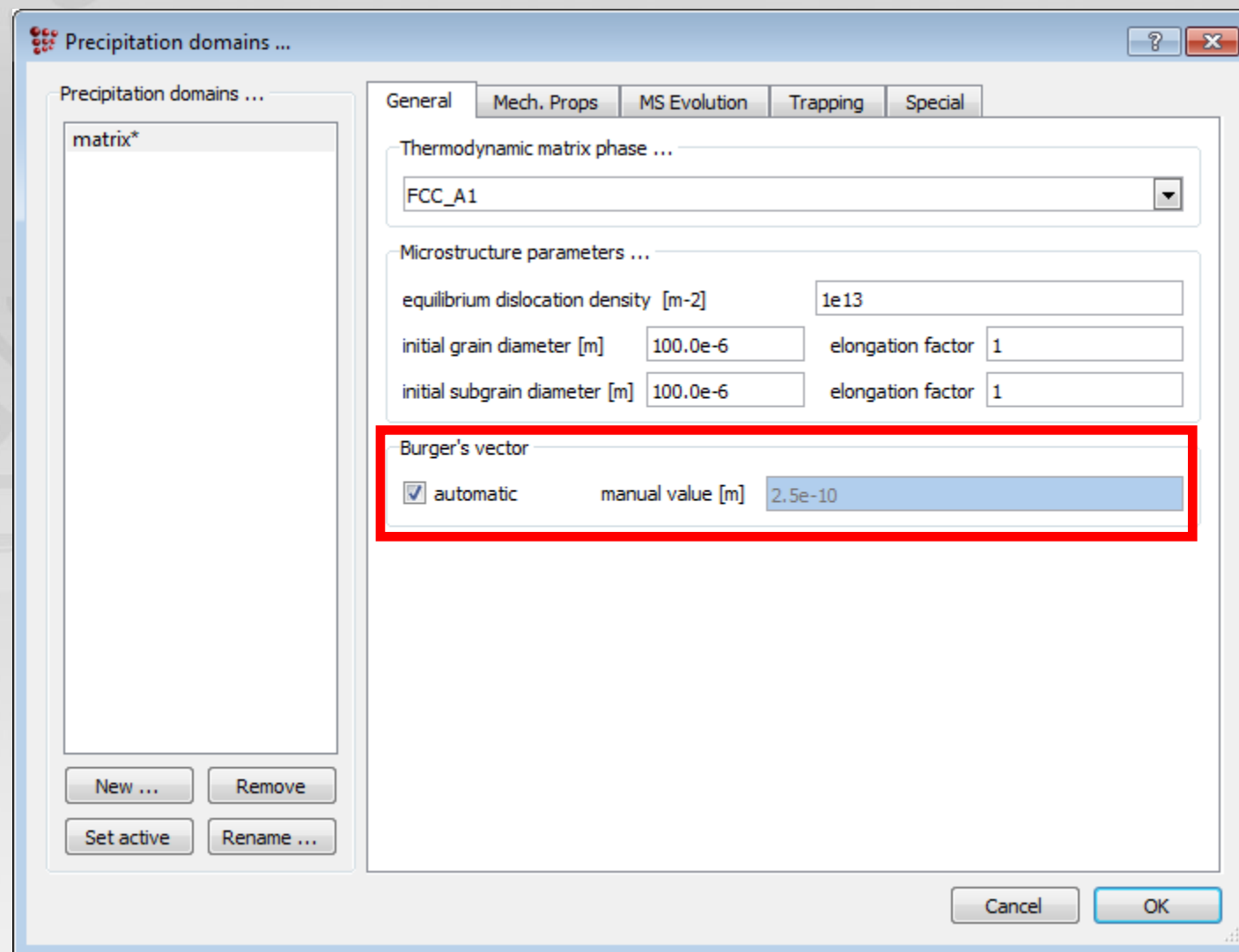
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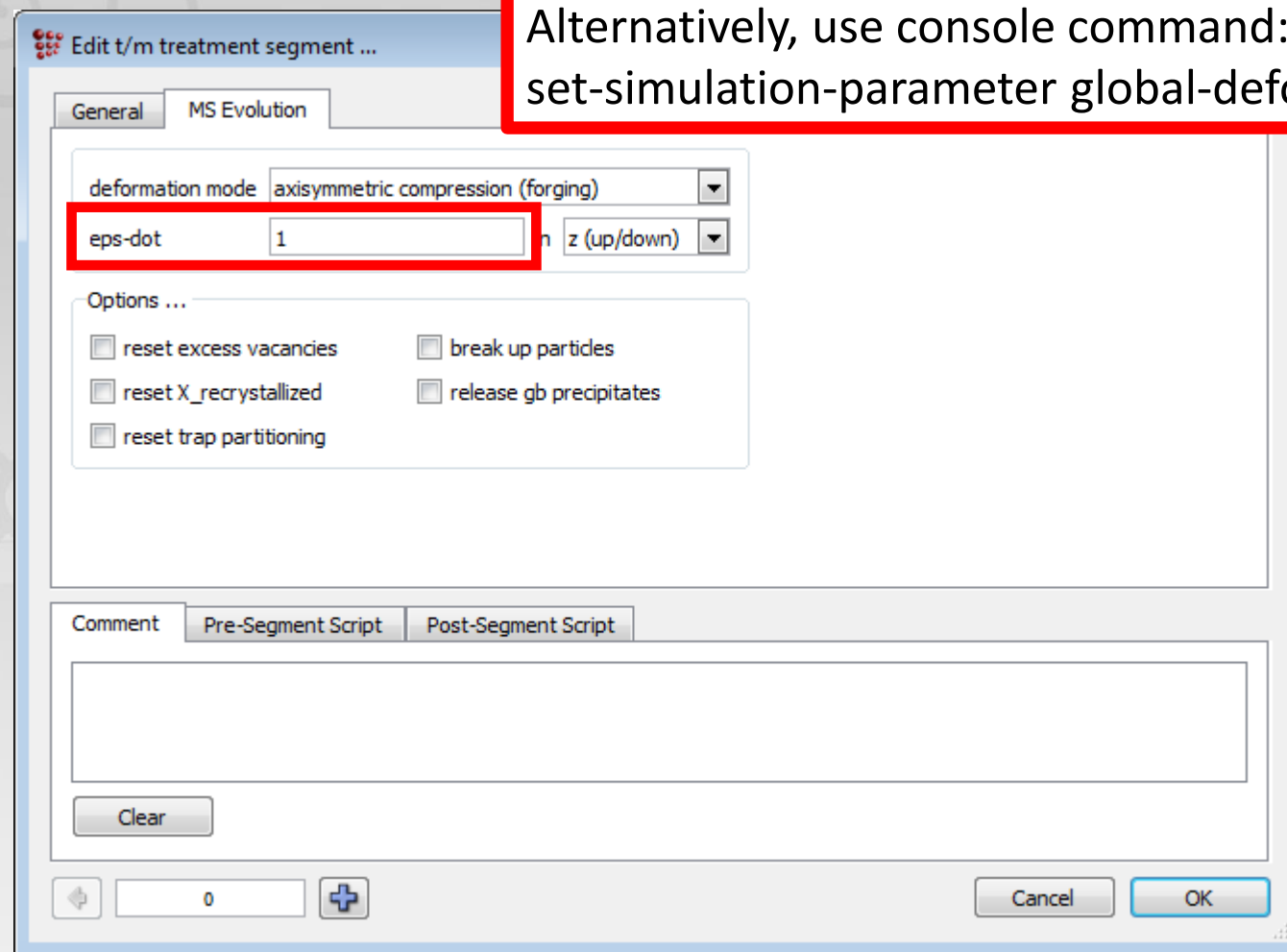
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Alternatively, use console command:  
set-simulation-parameter global-deformation-rate=1



# Dislocation density evolution

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# Dislocation annihilation (dynamic recovery)

$$\dot{\rho}_2 = \boxed{B} \frac{2M d_{ann}}{b} \dot{\epsilon} \rho$$

$B$  - B-parameter (constant)

$d_{ann}$  - Annihilation distance

Precipitation domains ...

matrix\*

General Mech. Props MS Evolution Trapping Special

Grainstructure Substructure Solute drag Vacancies Heat generation

Substructure evolution model 1-param - Sherstnev-Lang-Kozeschnik - 'ABC'

Excess dislocations ...

Rho\_total [m-2] 0

Equilibrium wall dislocation density ...

from Read-Shockley / manual 1e14 Misorientation [deg] 3

SGB pinning force ...

include disl. pinning cell width [m] 1e-8

Dislocation generation and annihilation ...

Parameter	Value	Description
A	50	Mean free path for dislocation generation
B	5	Dislocation annihilation coefficient (DRV)
C	1e-3	Dislocation annihilation coefficient (SRV)
A'	30	Similitude parameter. Similar to A. but not totally

New ... Remove

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# Dislocation annihilation (dynamic recovery)

$$d_{ann} = \frac{Gb^4 N_A}{2\pi(1 - \nu)E_{Va}}$$

$d_{ann}$  - Annihilation distance

$G$  - Shear modulus

$\nu$  - Poisson ratio

$E_{Va}$  - Vacancy formation energy

(from thermodynamic database)

$N_A$  - Avogadro constant

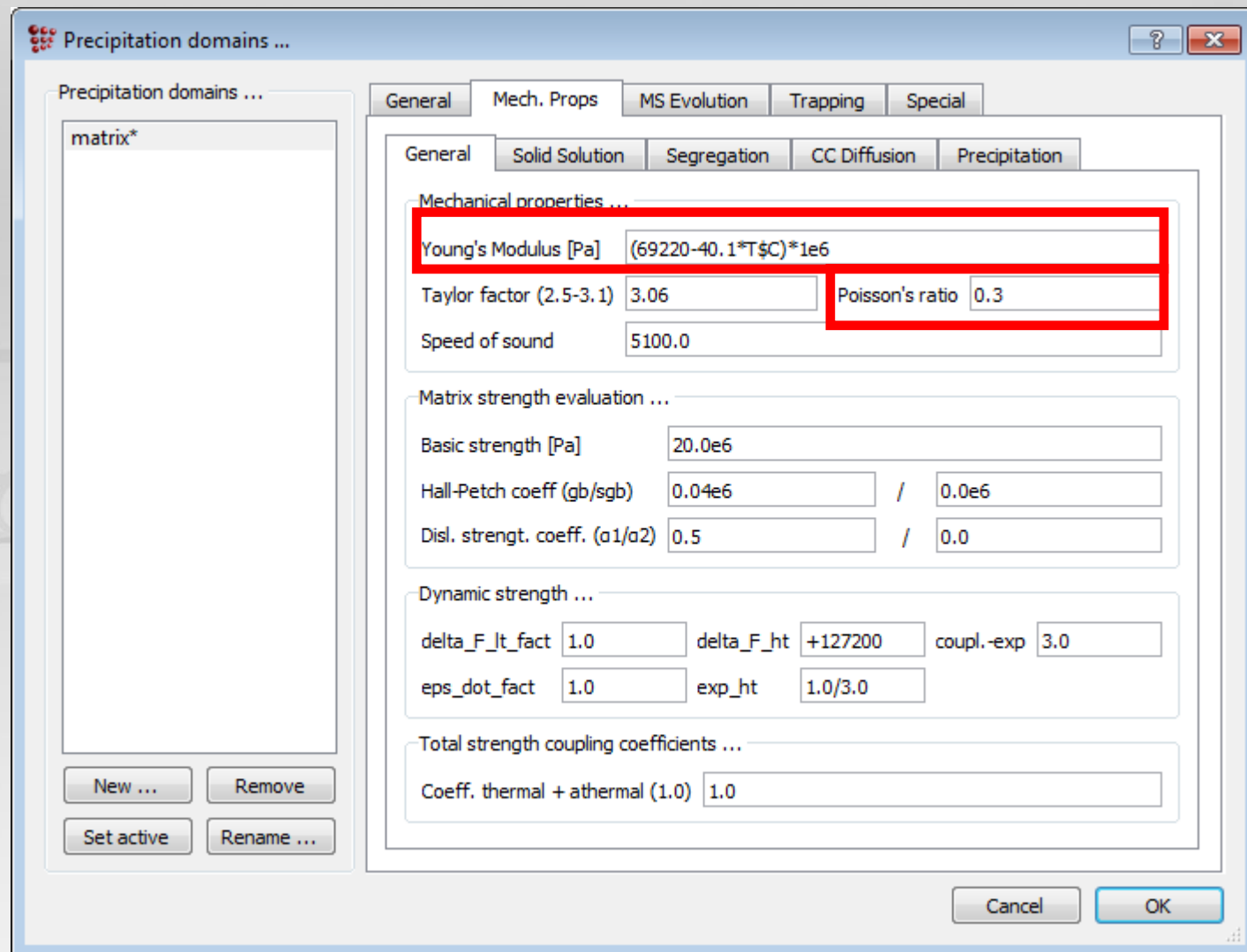
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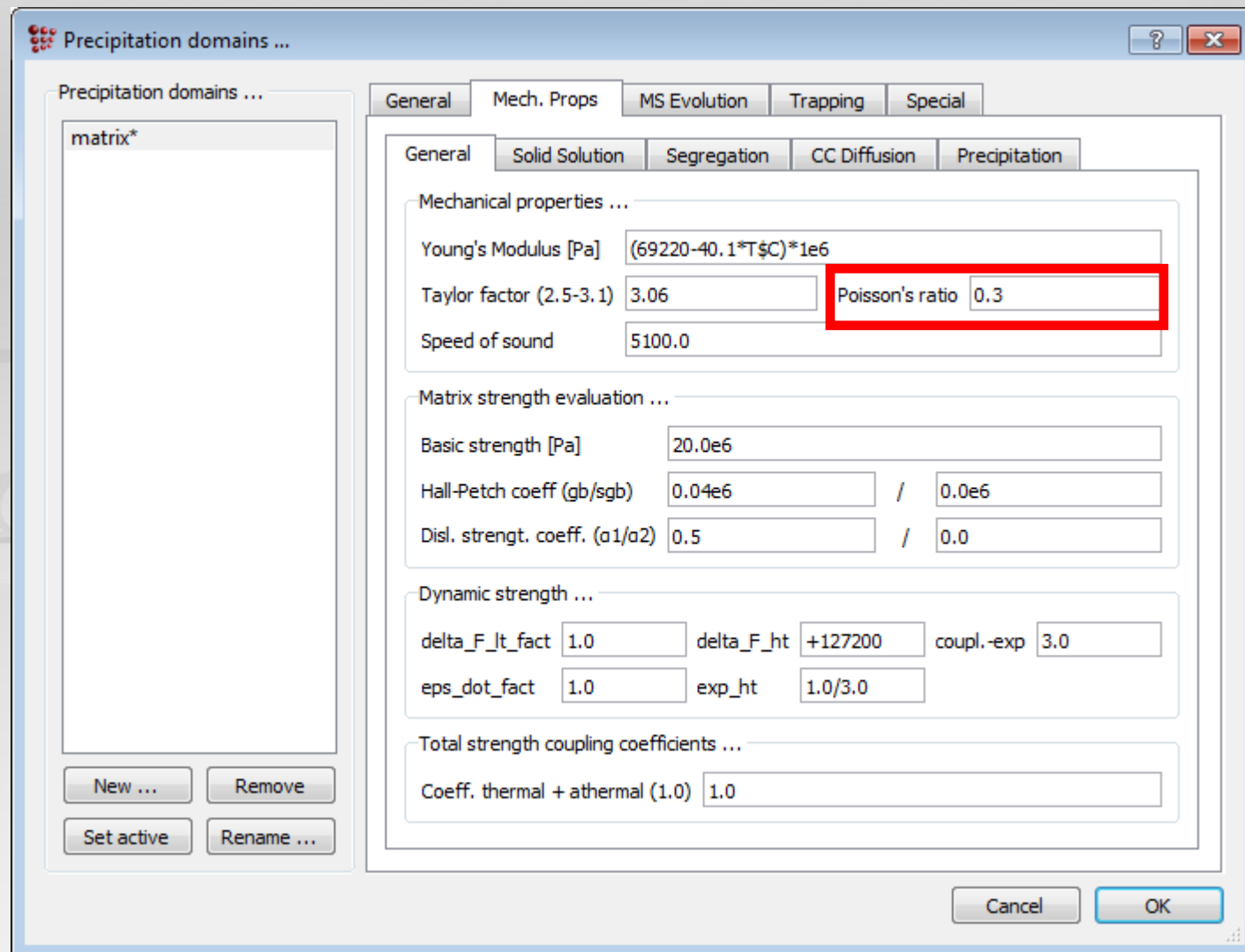
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# Dislocation annihilation (static recovery)

$$\dot{\rho}_3 = C \frac{2Gb^3 D_{eff}}{k_B T} (\rho^2 - \rho_{eq}^2)$$

$D_{eff}$  - Effective diffusion coefficient, incl. enhancement factors like pipe diffusion, excess vacancies, etc.

$k_B$  - Boltzmann constant

$C$  - C-parameter (constant)

$T$  - Temperature

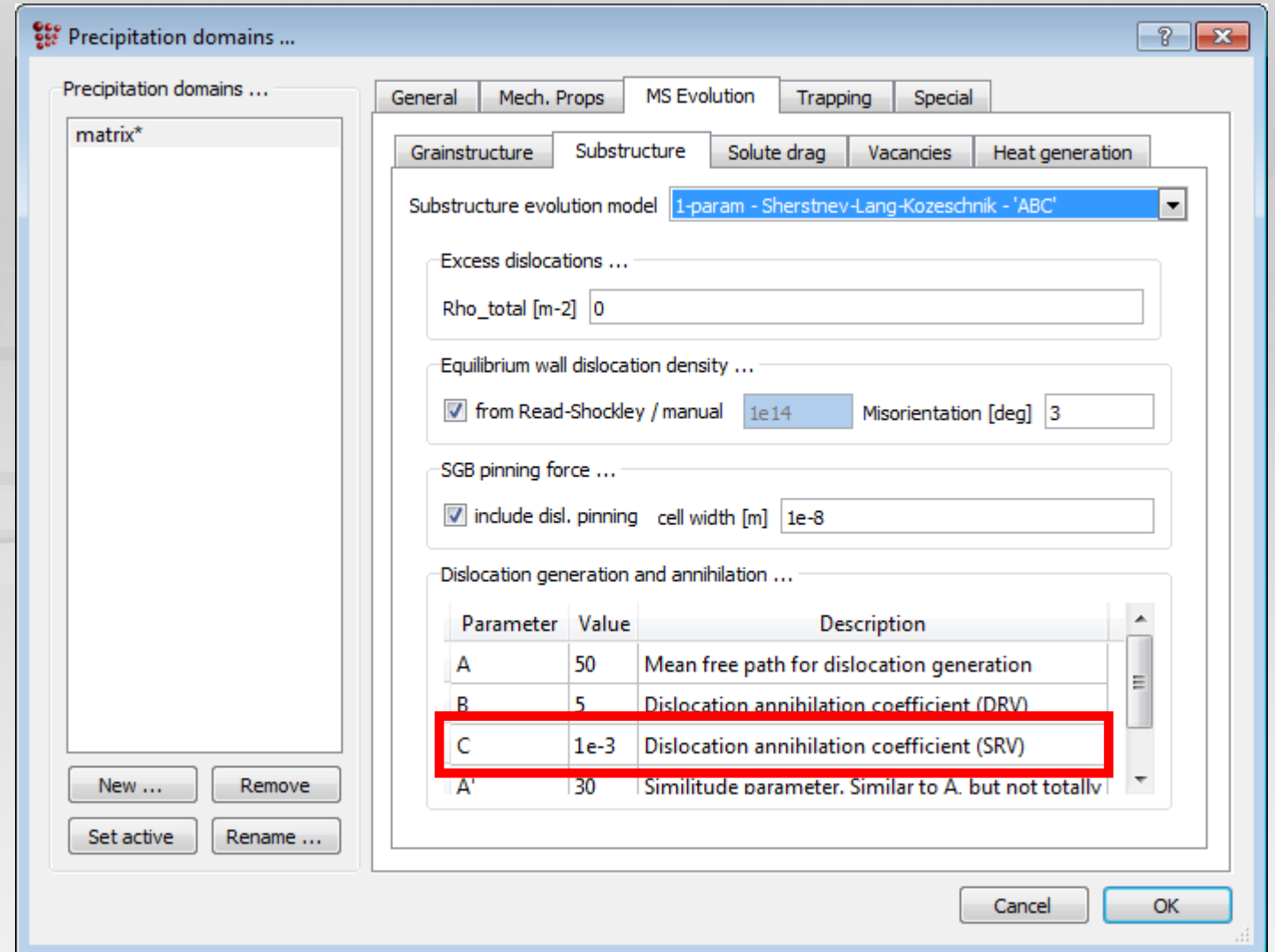
$\rho_{eq}$  - Equilibrium dislocation density

# Dislocation annihilation (static recovery)

$$\dot{\rho}_3 = C \frac{2Gb^3 D_{eff}}{k_B T} (\rho^2 - \rho_{eq}^2)$$

$C$  - C-parameter (constant)

$\rho_{eq}$  - Equilibrium dislocation density  
(sum of equilibrium values for  
intrinsic and wall dislocations)

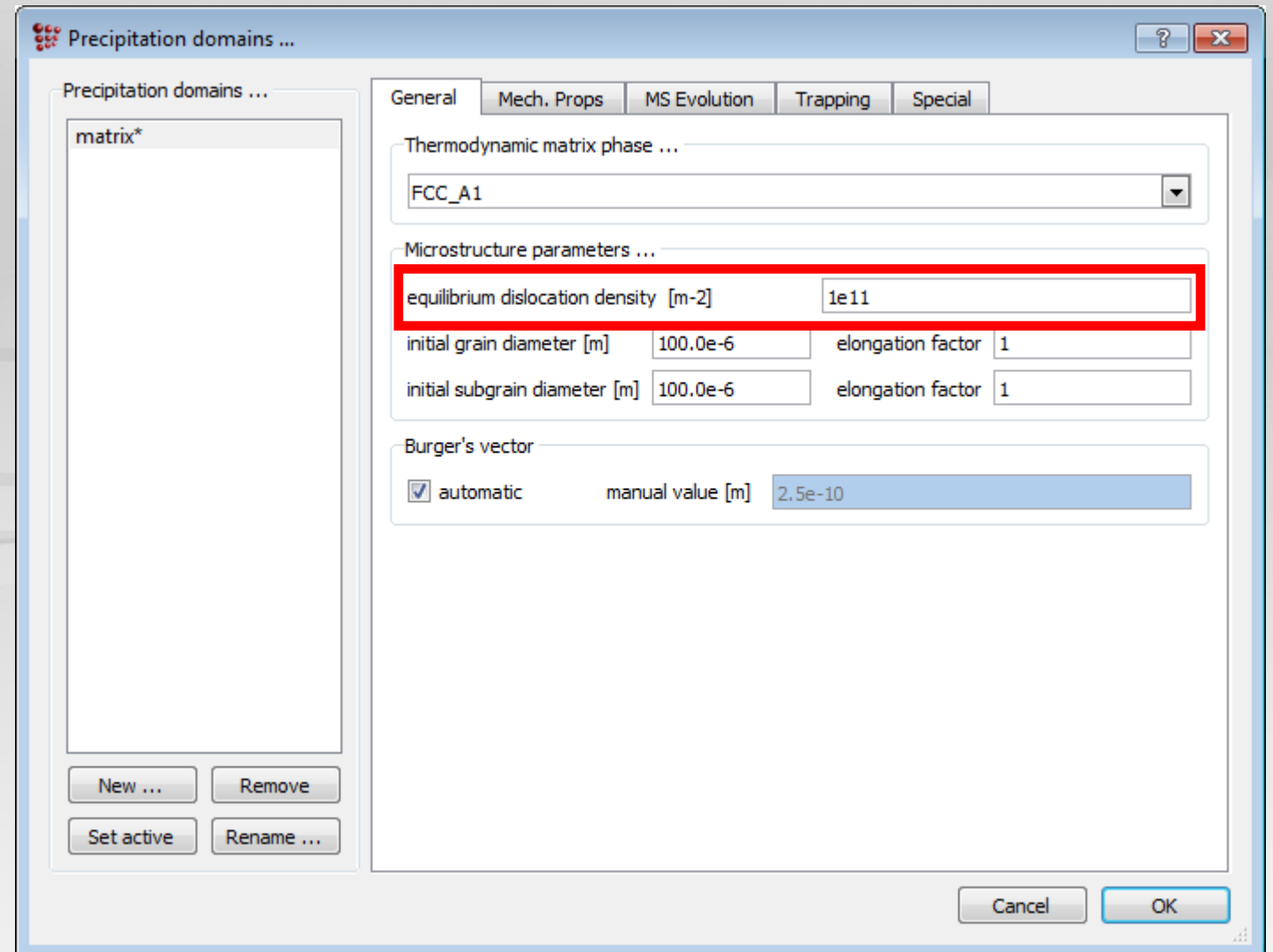


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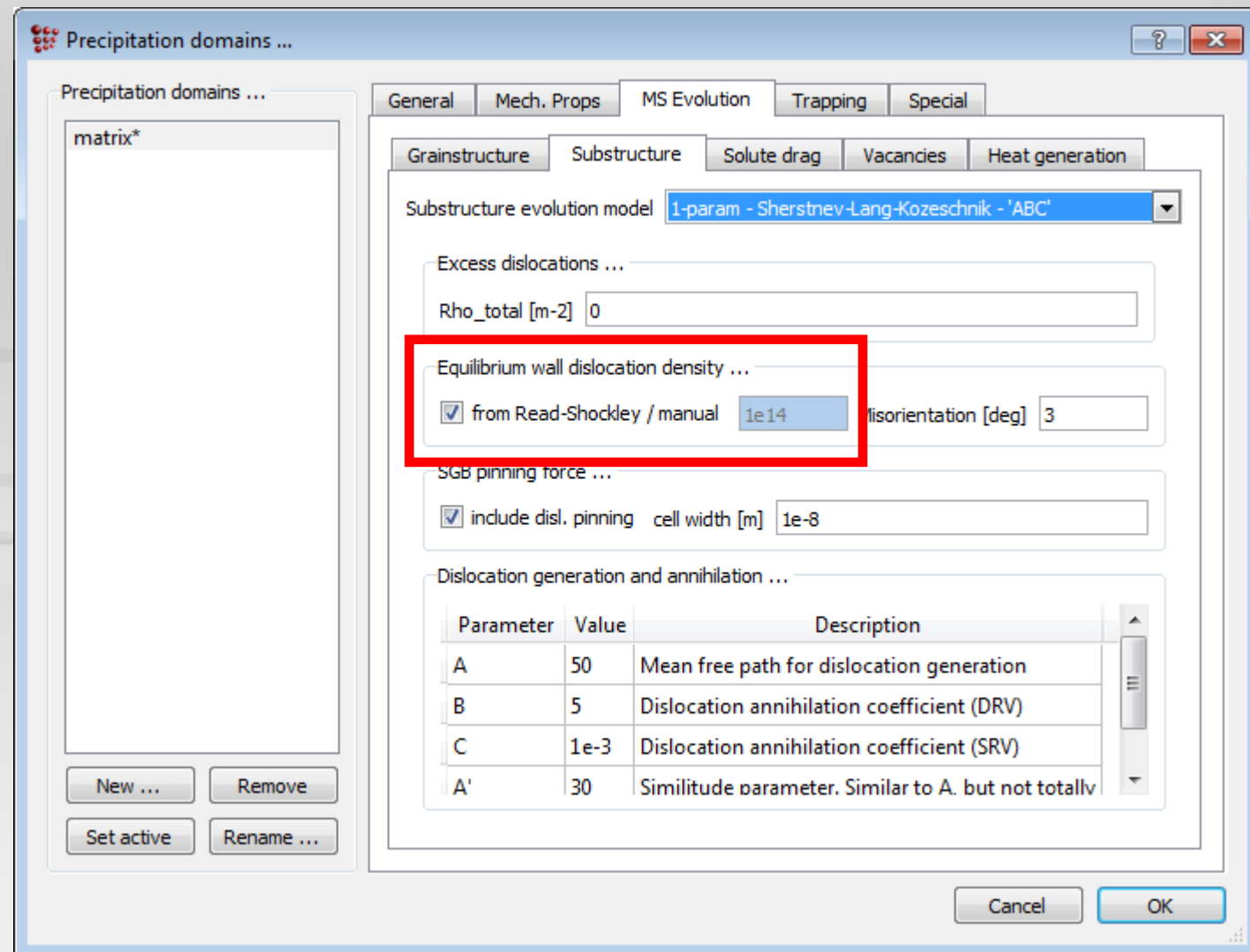


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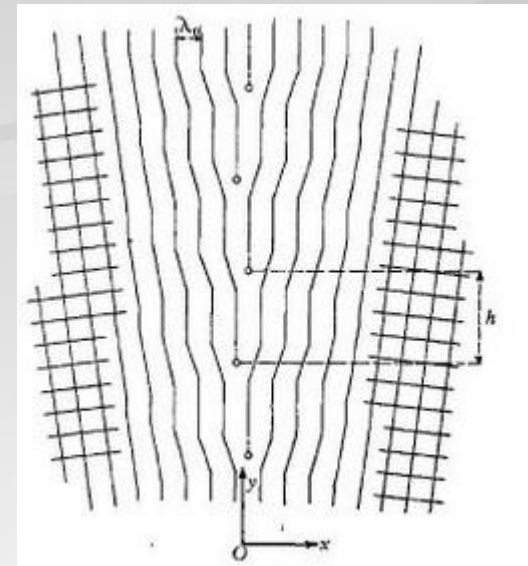
# Wall dislocation density (1-parameter model)

- Taken as Read-Shockley dislocation density  $\rightarrow$  necessary amount to fulfill geometrical constraint for subgrains with a given misorientation angle and size

$$\rho_{RS} = \frac{\tan\theta}{\delta b}$$

$\theta$  - Misorientation angle

$\delta$  - Subgrain diameter



Burgers, J.M., Proc. Phys. Soc. 52 (1940) 23-33

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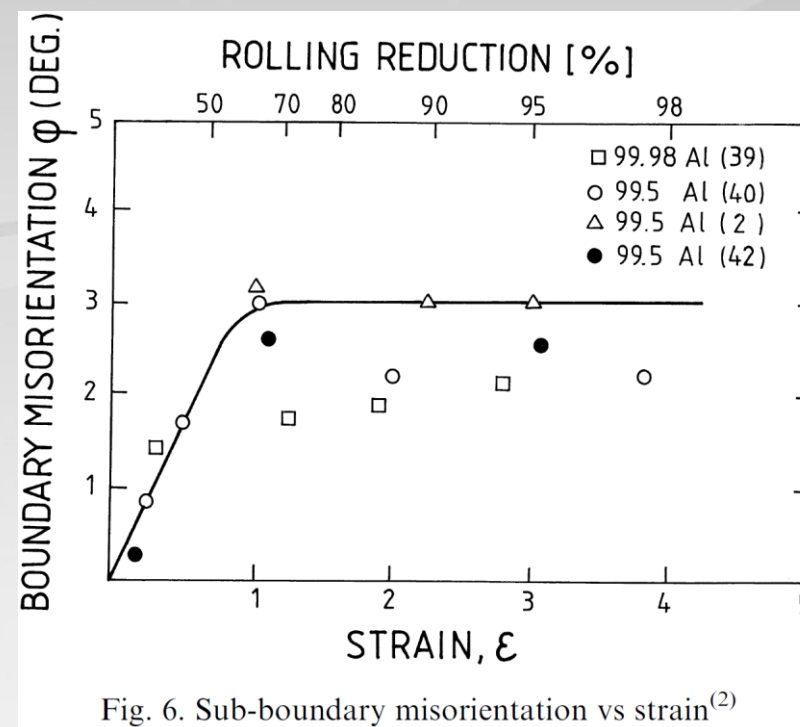


Fig. 6. Sub-boundary misorientation vs strain<sup>(2)</sup>

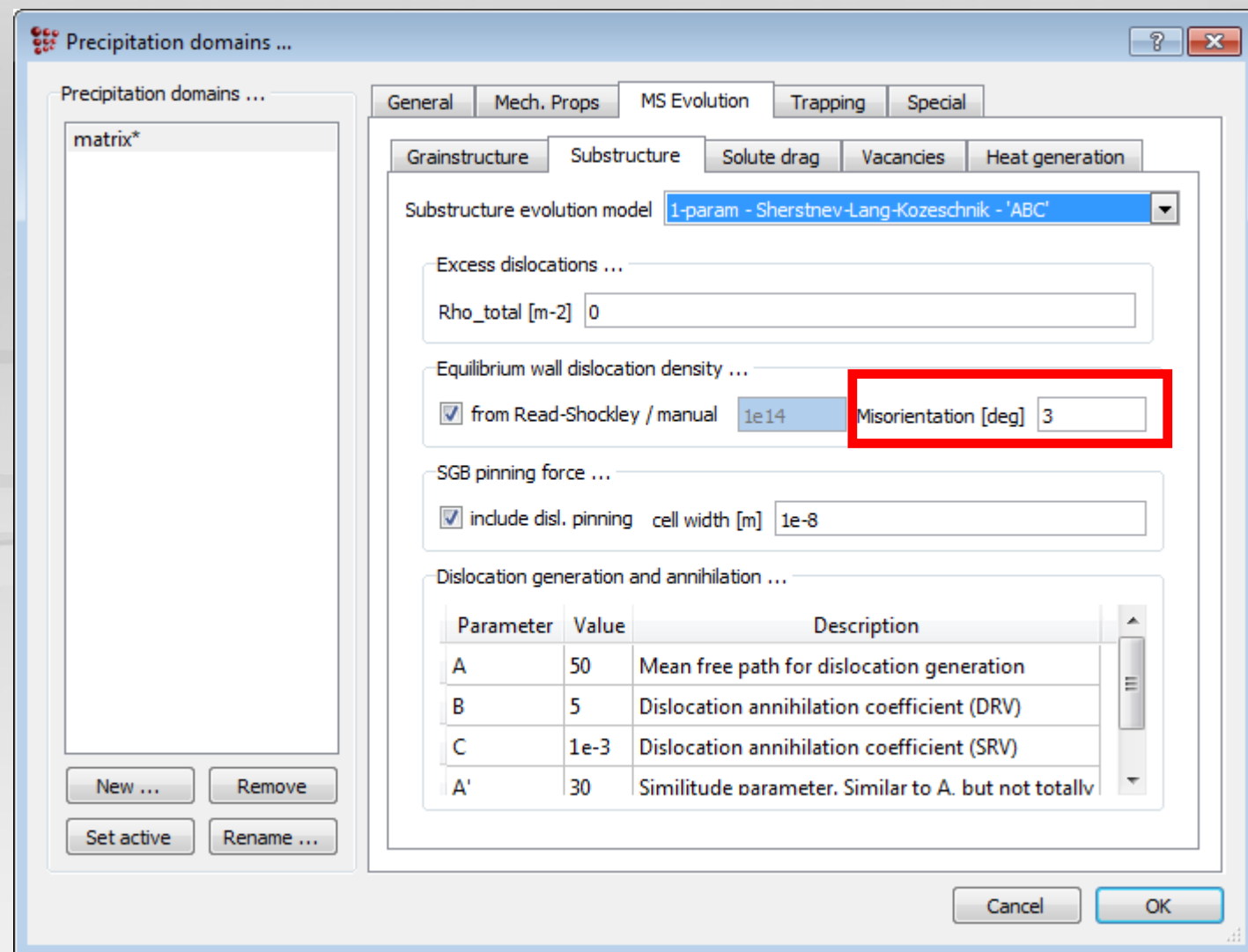
E. Nes, Prog. Mater. Sci. 41 (1998) p.129-193

# Read-Shockley dislocation density

Read-Shockley dislocation density  
 → necessary amount to fulfill geometrical constraint

$$\rho_{RS} = \frac{\tan \theta}{\delta b}$$

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# Wall dislocation density (2-parameter model)

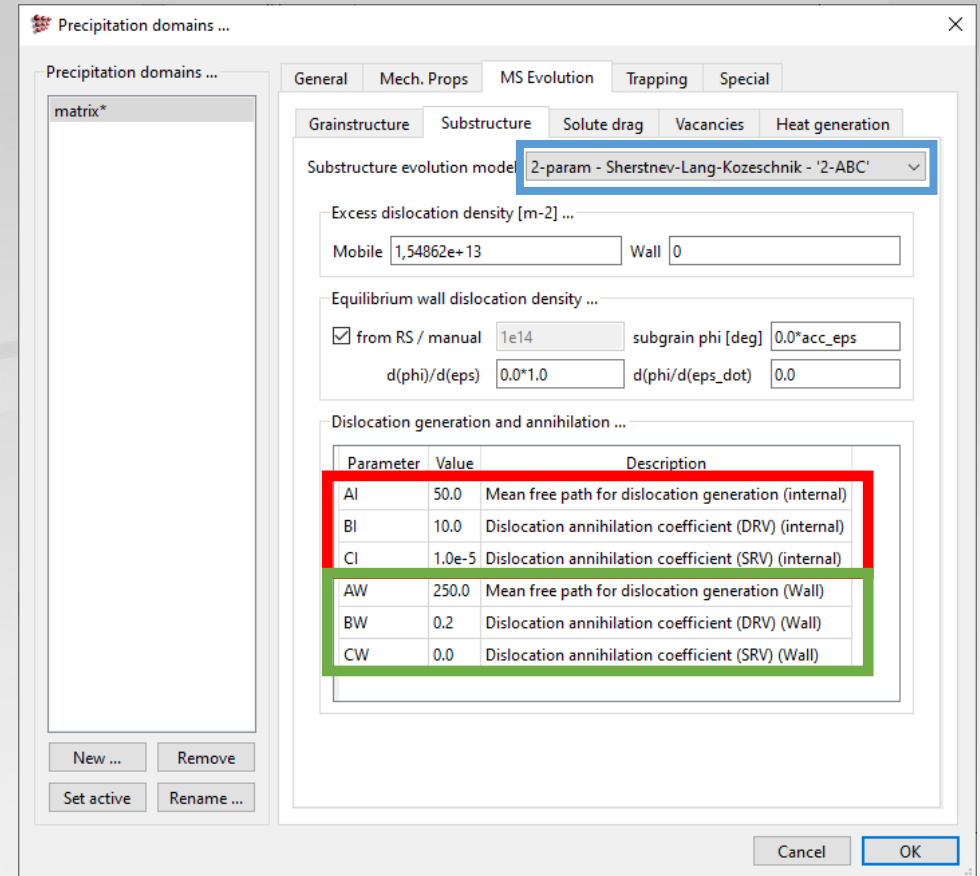
- Separate equations for internal and wall dislocations

- Internal dislocations

$$\dot{\rho}_i = \rho_{i,1} - \rho_{i,2} - \rho_{i,3}$$

- Wall dislocations

$$\dot{\rho}_w = \rho_{w,1} - \rho_{w,2} - \rho_{w,3}$$





# Subgrain size evolution

(only when a subgrain evolution model is active)

# Subgrain size evolution

$$\dot{\delta} = \dot{\delta}_1 - \dot{\delta}_2$$

- Subgrains grow to minimize the subgrain boundary area (minimize the boundary energy)  $\rightarrow \dot{\delta}_1$
- Subgrain walls shrink with increasing dislocation density (more wall dislocations available)  $\rightarrow \dot{\delta}_2$

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# Subgrain growth

$$\dot{\delta}_1 = MP_D$$

- Subgrain growth model same as for grain growth → product of mobility and driving force
- Same models for growth inhibition as for grain boundary mobility → same effects for precipitate pinning and solute drag

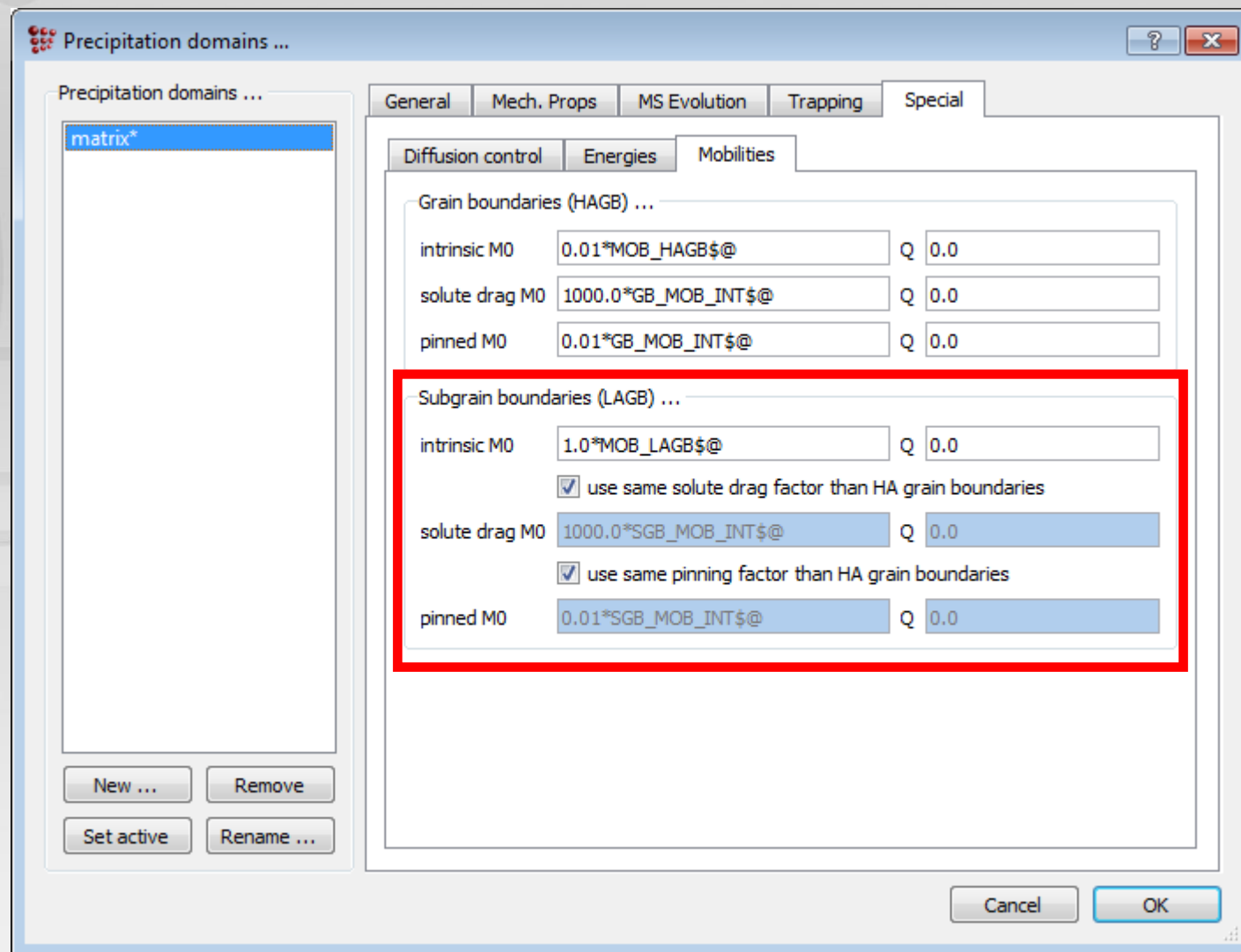
# Subgrain growth

$$\dot{\delta}_1 = M P_D$$

$$M = \eta_f \frac{D_b b^2}{k_b T}$$

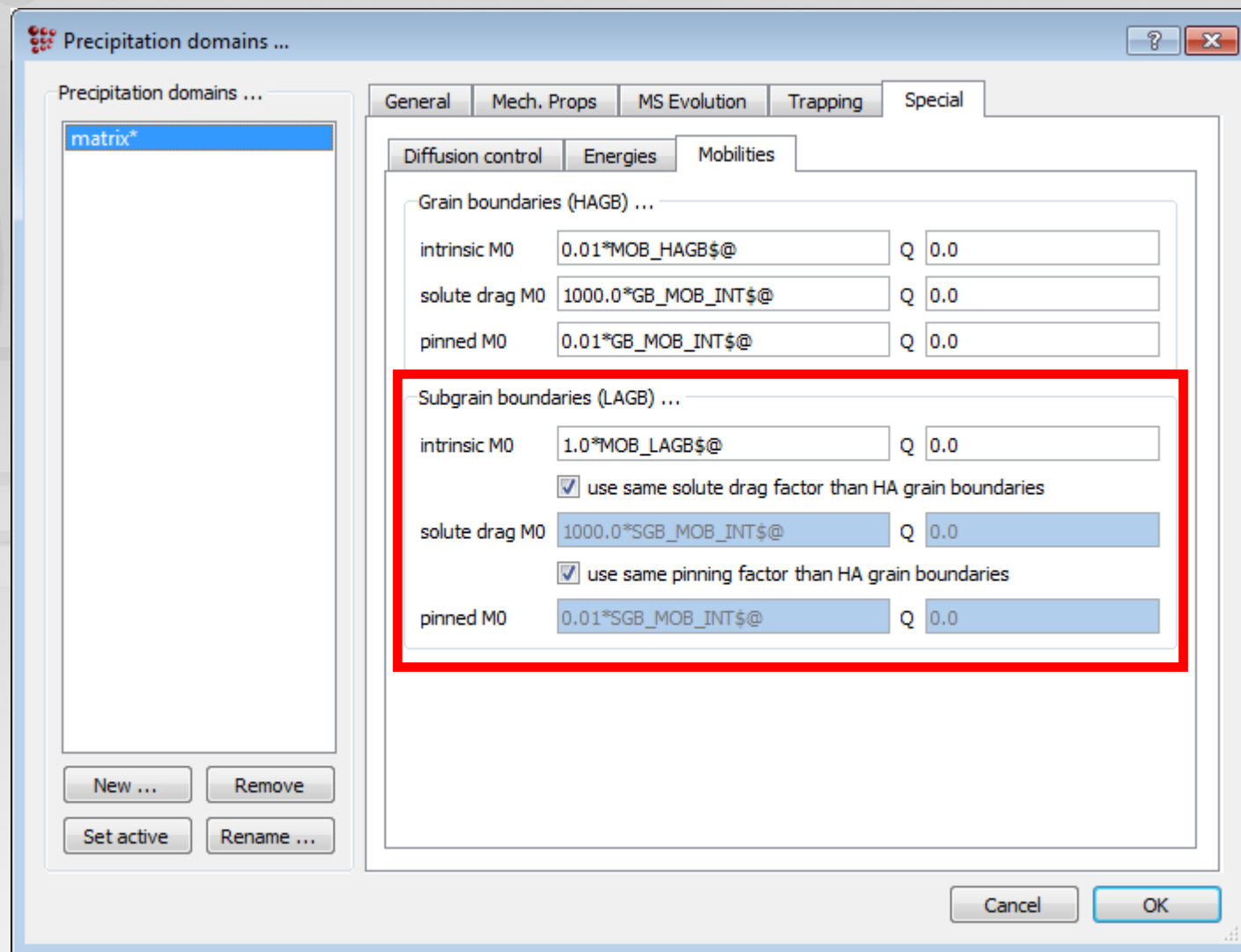
$D_b$  - Bulk diffusion coefficient

$\eta_f$  - Scaling factor



# Subgrain growth

$$\dot{\delta}_1 = M P_D$$



Same models as for grain boundary mobility

→ same effects for precipitate pinning and solute drag

# Subgrain growth

- Driving force – balance between Laplace pressure and dislocation pinning of subgrain walls

$$P_D = \frac{4\gamma_{sgb}}{\delta} - \frac{Gb^2}{\sqrt{w\rho}} \sqrt{\rho - \rho_{RS}}$$

$\gamma_{sgb}$  - Subgrain boundary energy

$\delta$  - Subgrain size

$w$  - Cell width for dislocation pinning

$\rho_{RS}$  - Read-Shockley dislocation density

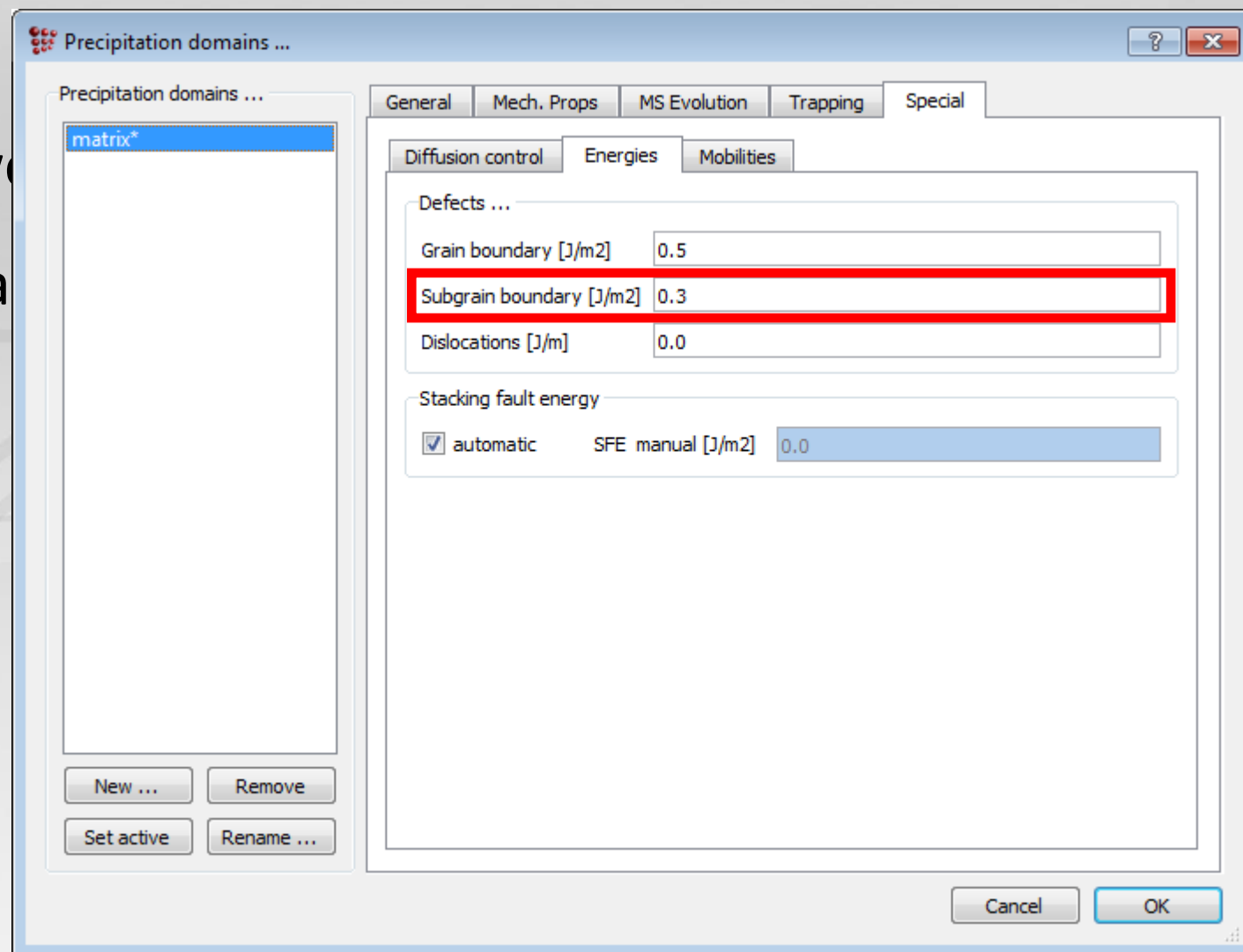
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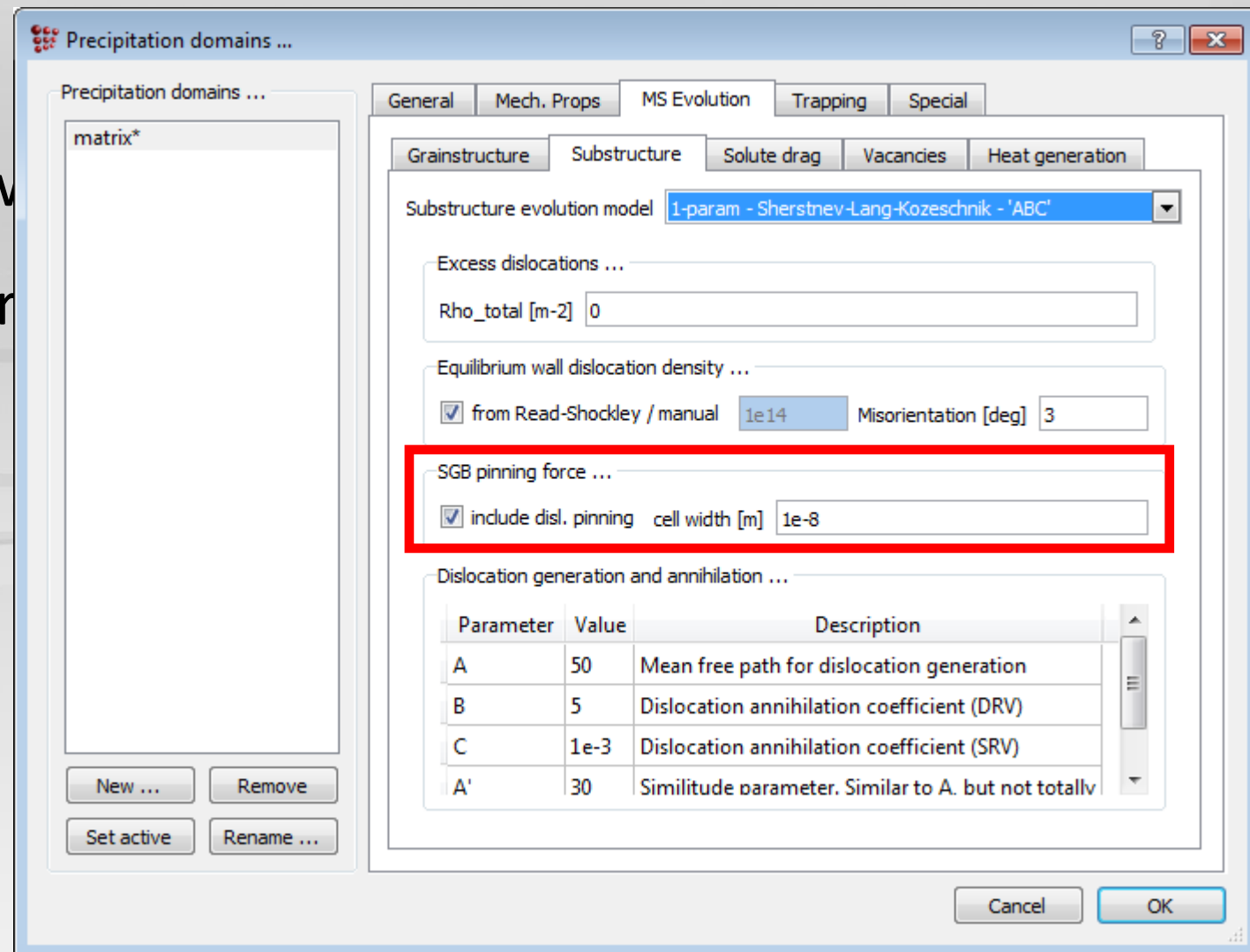


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- Driving force – balance between grain boundary energy and dislocation pinning of subgrains

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$w$  - Cell width for dislocation pinning



# Subgrain size evolution

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# Subgrain shrinkage

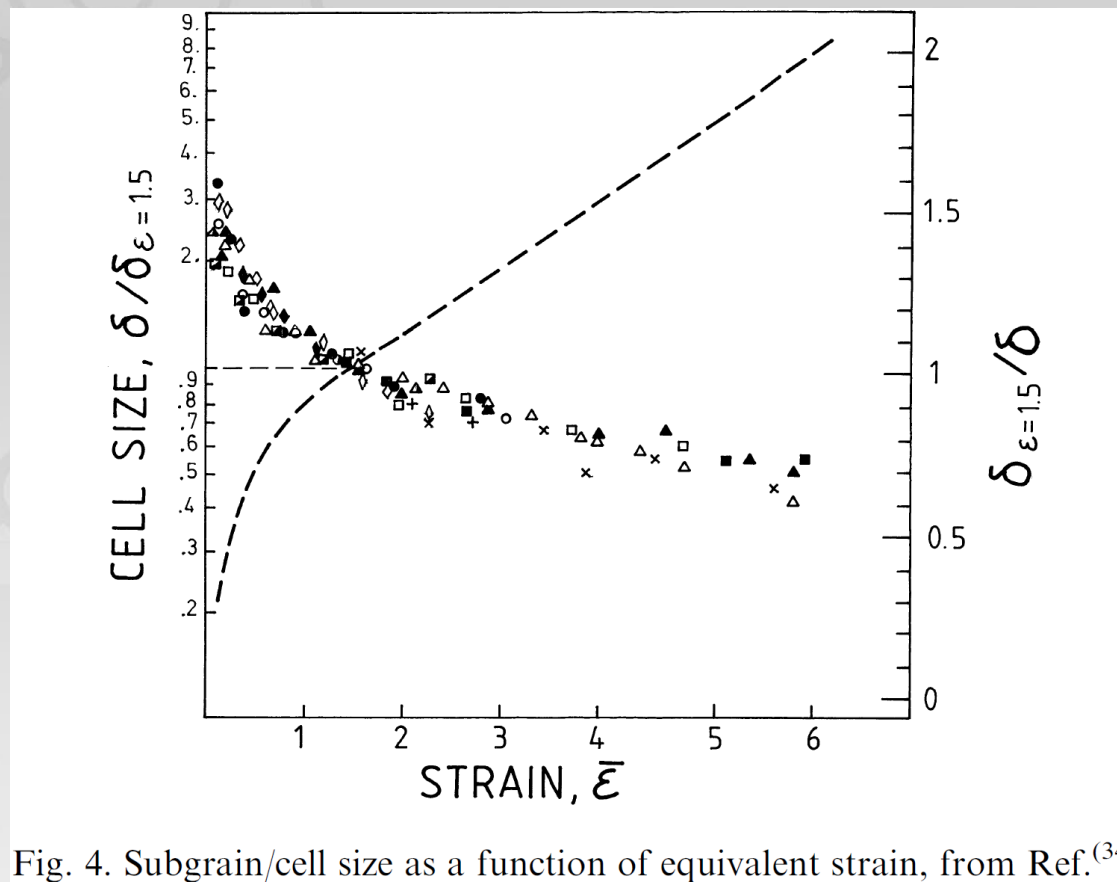


Fig. 4. Subgrain/cell size as a function of equivalent strain, from Ref.<sup>(34)</sup>

E. Nes, Prog. Mater. Sci. 41 (1998) p.129-193

# Subgrain shrinkage

$$\dot{\delta}_2 = \frac{\delta^3}{2(A')^2} \dot{\rho}_1$$

$A'$  -  $A'$ -parameter (constant)

Precipitation domains ...

matrix\*

General Mech. Props MS Evolution Trapping Special

Grainstructure Substructure Solute drag Vacancies Heat generation

Substructure evolution model 1-param - Sherstnev-Lang-Kozeschnik - 'ABC'

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# Acknowledgments

- Yao Shan
- Heinrich Buken



Thank you for  
your attention!

